



# Directly Revocable Key-Policy Attribute-Based Encryption with Verifiable Ciphertext Delegation

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## Traditional Encrypted Filesystem





File 1

Owner: John

➤ Encrypted Files stored on Untrusted

Server

File 2

Owner: Tim

> Every user can decrypt its own files

> Files to be shared across different users? Credentials?





## **Key-Policy Attribute-Based Encryption**



#### File 1

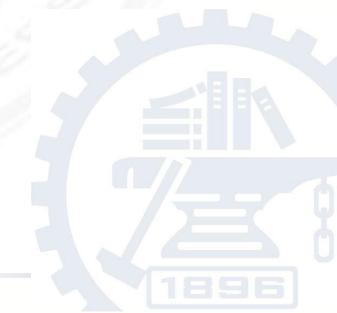
- "Creator: John"
- •"Computer Science"
- "Admissions"
- •"Date: 04-11-06"

➤ Label files with attributes



#### File 2

- •"Creator: Tim"
- •"History"
- "Admissions"
- •"Date: 03-20-05"





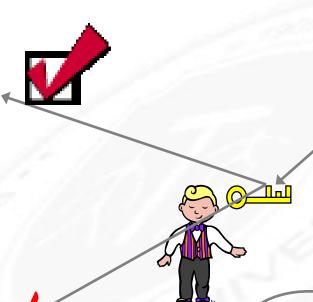


## Key-Policy Attribute-Based Encryption



#### File 1

- "Creator: John"
- "Computer Science"
- •"Admissions"
- •"Date: 04-11-06"



OR



#### File 2

- •"Creator: Tim"
- •"History"
- •"Admissions"
- •"Date: 03-20-05"



"Bob"

Univ. Key

**Authority** 

"Computer Science"

"Admissions"

4





#### Our Work (1/4): Revocation

- Guarantees
- Non-revoked users can decrypt data.
- Revoked users can't decrypt data added in the future.
- Revoked users can't decrypt data in the past.
   [22] (After termination, employee shouldn't be able to access anything he doesn't already have)

[22] A. Sahai, H. Seyalioglu, B. Waters, Dynamic credentials and ciphertext delegation for attribute-based encryption, in: CRYPTO, 2012, pp. 199-217.





## Our Work (2/4): Revocation

- Non-revoked users can decrypt data.
- Revoked users can't decrypt data added in the future.
  - Direct mode: no need to update non-revoked users' decryption keys.
  - ✓ Indirect mode: need to update all the non-revoked users' decryption keys.





## Our Work (3/4): Revocation

- Revoked users can't decrypt data in the past.
  - ✓ Update the past encrypted data
    - Traditional way: The data owner must download, decrypt, re-encrypt and upload the data stored in the cloud.
    - ➤ Outsourcing to cloud: The cloud update the encrypted data- "ciphertext delegation".
      - ➤ Unverifiable: the process can't be accountable.
      - Verifiable: the process can be accountable.





#### Our Work (4/4): Revocation

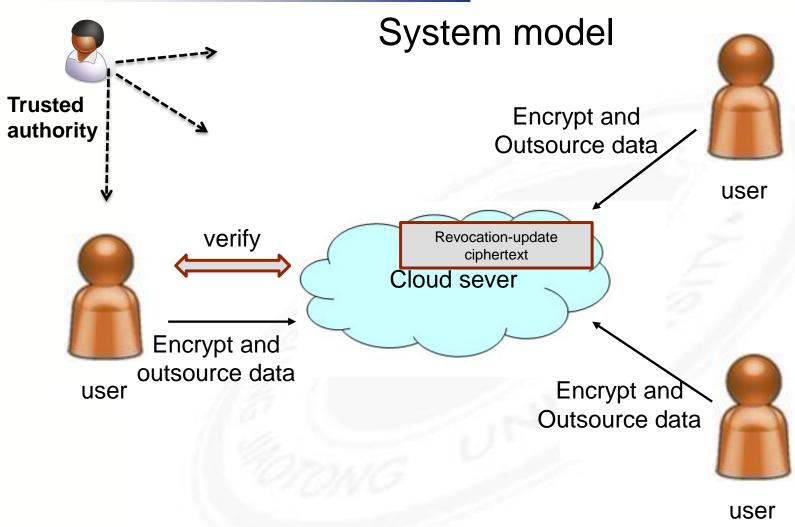
Scheme	Direct revocation	Ciphertext delegation	Update verifiability	Security assumption
Scheme 1 [2]	$\checkmark$	×	×	n-BDHE
Scheme 2 [2]	<b>√</b>	×	×	r-MEBDH
[1]	$\checkmark$	×	×	DBDH
[5]	×	×	×	DBDH
[22]	×	<b>√</b>	×	three static assumptions
Our solution	$\checkmark$	<b>√</b>	<b>√</b>	(d+3)-MDDH

Table 1: Property summary for revocable KPABE schemes in the literature and the solution in this paper. Direct revocation means that the trusted authority can solely update revocation list and there is no need to update non-revoked users' decryption key. Ciphertext delegation means that ciphertexts can be updated by the third party correspondingly when the revocation list is updated. Update verifiability means that the process of the third party updating ciphertexts can be accountable.

- [1] N. Attrapadung, H. Imai, Attribute-based encryption supporting direct/indirect revocation modes, in: IMA Int. Conf., 2009, pp. 278-300.
- [2] N. Attrapadung, H. Imai, Conjunctive broadcast and attribute-based encryption, in: Pairing-Based Cryptography–Pairing 2009, Springer, 2009, pp. 248–265.
- [5] A. Boldyreva, V. Goyal, V. Kumar, Identity-based encryption with efficient revocation, in: ACM Conference on Computer and Communications Security, 2008, pp. 417-426.
- [22] A. Sahai, H. Seyalioglu, B. Waters, Dynamic credentials and ciphertext delegation for attribute-based encryption, in: CRYPTO, 2012, pp. 199-217.











## **Techniques**

- Techniques
  - Multilinear Maps
  - Subset cover





#### Multilinear Maps

$$d + 3: (G_0, G_1, ..., G_{d+2})$$
 order  $p$ 

$$d+2$$
 mappings  $e_i:G_0\times G_i\to G_{i+1}, i=0,\ldots,d+1$ 

#### Properties:

✓ Given generator  $g_0 \in G_0$ , then  $g_{i+1} = e_i(g_0, g_i)$  is the generator of  $G_{i+1}$ 

$$\checkmark e_i(g_0^{\alpha}, g_i^{\beta}) = e_i(g_0, g_i)^{\alpha\beta}$$

 $\checkmark e_i$  can be efficiently computed





#### **Subset Cover**

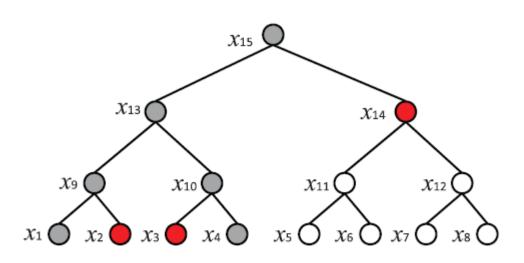


Figure 1: Subset cover technique to encode the revocation list. Given the revocation list  $R = \{x_1, x_4\}$ , the nodes of  $path(x_1)$  and  $path(x_4)$  are marked (in gray color), and then  $cover(R) = \{x_2, x_3, x_{14}\}$  (in red color).





#### System Setup





 $\alpha, \beta \stackrel{R}{\leftarrow} Z_p, H_1: \{0,1\}^* \to Z_p, H_2: \{0,1\}^* \to G_0,$ 

 $h_j \stackrel{R}{\leftarrow} G_{d+1}, 0 \le j \le max, max$  is the maximum number

of attributes. Define  $Q(y) = \prod_{j=0}^{max} (h_j^{y^j}), y \in Z_p$ 



$$pm = (e_0, ..., e_{d+1}, G_0, ..., G_{d+2}, g_0, ..., g_{d+2}, e_{d+1}(g_0, g_{d+1})^{\alpha}, g_0^{\beta}, H_1, H_2, h_0, ..., h_{max})$$



 $mk=(\alpha,\beta)$ 





#### **Key Generation**



$$mk = (\alpha, \beta)$$

(1) 
$$\alpha_1, v_2, v_3, \dots, v_k \stackrel{R}{\leftarrow} Z_p$$
, set  $\alpha_2$ , s.t.  $\alpha = \alpha_1 + \alpha_2 \mod p$ .

(2) 
$$\mathbf{v} = (\alpha_1, v_2, v_3, ..., v_k),$$

for i = 1, ..., l, compute  $\lambda_{\pi(i)} = M_i \cdot \mathbf{v}$ , M is an  $l \times k$  matrix

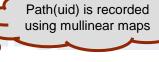
$$D_i^{(1)} = g_{d+1}^{\lambda_{\pi_{(i)}}} Q(H_1(\pi(i)))^{r_i}, D_i^{(2)} = g_0^{r_i}, r_i \stackrel{R}{\leftarrow} Z_p;$$

(3) Let  $P_{x_{i_0}} = e_0(H_2(x_{i_0}), g_0^{\beta})$ , compute  $P_{x_{i_j}} = e_j(H_2(x_{i_j}), P_{x_{i_{j-1}}})$ ,

where j = 1, ..., d. (path(uid)= $\{x_{i_0}, ..., x_{i_d}\}$ )

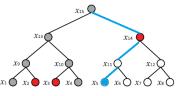
$$D^{(3)} = g_{d+1}^{\alpha_2} P_{\mathrm{uid}}^t$$
 ,  $D^{(4)} = g_0^t$  ,  $t \stackrel{R}{\leftarrow} Z_p$  ;

 $sk = (uid, (M,\pi), (D_i^{(1)}, D_i^{(2)})_{i \in [1,l]}, D^{(3)}, D^{(4)})$ 



Access control

policy







## Encryption



$$pm = (e_0, ..., e_{d+1}, G_0, ..., G_{d+2}, g_0, ..., g_{d+2}, e_{d+1}(g_0, g_{d+1})^{\alpha}, g_0^{\beta}, H_1, H_2, h_0, ..., h_{max})$$



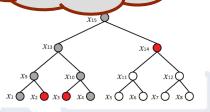
Encrypt the massage  $m \in G_{d+2}$  under attribute set S

(1) 
$$C^{(1)} = \text{m}e_{d+1}(g_0, g_{d+1})^{\alpha s}, C^{(2)} = g_0^s, s \stackrel{R}{\leftarrow} Z_p;$$
(2)  $C_{\text{at}}^{(3)} = Q(H_1(\text{at}))^s, \text{at } \in S;$ 

(3)  $\operatorname{path}(x) = \{x_{i_0}, \dots, x_{i_{depth(x)}}\}, x_{i_0} = root \land x_{i_{depth(x)}} = x, x \in cover(R), cover(R) \text{ is the cover set of revocation list R.}$ 

$$P_{x_{i_0}} = e_0(H_2(x_{i_0}), g_0^{\beta})$$
, compute  $P_{x_{i_j}} = e_j(H_2(x_{i_j}), P_{x_{i_j}})$ , where  $j = 1, ..., dept(x)$ , set  $C_x^{(4)} = P_x^S$ . The set cover nodes

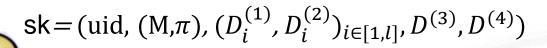
cph=(S,R,
$$C^{(1)}$$
,  $C^{(2)}$ ,{ $C^{(3)}_{at}$ }<sub>at∈S</sub>,{ $C^{(4)}_x$ }<sub>x∈cover(R)</sub>)

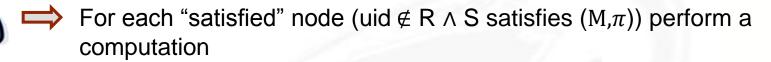






#### **Decryption Part I**





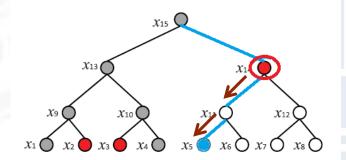
(1) With uid  $\notin$  R, exist a node x s. t.  $x \in (path(uid) \cap cover(R))$ , suppose

path(uid) = 
$$\{x_{i_0}, ..., x_{i_{depth(x)}}, ..., x_{i_d}\}, x_{i_d} = \text{uid } \land x_{i_{depth(x)}} = x;$$

(2) Let 
$$P'_{x_{i_{depth(x)}}} = C_x^{(4)}$$
, compute  $P'_{x_{j+1}} = e_{j+1}(H_2(x_{i_{j+1}}), P'_{x_{i_j}})$  for  $j = depth(x), \dots, d-1$ :

(3) 
$$P'_{uid} = P'_{x_{i_d}}$$

Extend ciphertext of x to uid (using multilinear maps)







#### **Decryption Part II**



(4) S satisfies (M, $\pi$ ), exist  $c_i$ , s.t.  $\sum_{\pi(i)\in S} c_i M_i = (1,0,...,0)$ , then

$$K = \prod_{\pi(i) \in S} \left( \frac{e_{d+1}(C^{(2)}, D_i^{(1)})}{e_{d+1}(D_i^{(2)}, C_{\pi(i)}^{(3)})} \right)^{c_i} \frac{e_{d+1}(C^{(2)}, D^{(3)})}{e_{d+1}(D^{(4)}, P'_{uid})}$$

(5)  $m = C^{(1)}/K$ .

S satisfies (M,  $\pi$ )

uid ∉ R





## Update

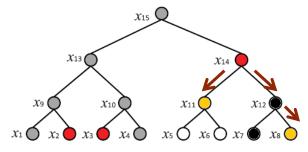


Given a new revocation list R', update as follows:

- If exists  $x \in \text{cover}(R)$  s.t. x = x', set  $\tilde{C}_{x'}^{(4)} = C_x^{(4)}$ ;
- Otherwise exists  $x \in \text{cover}(R)$  s.t. x is an ancestor of x', path $(x') = \text{path}(x) \cup \{x_{i_{depth(x)}}, \dots, x_{i_{depth(x')}}\}$ , where  $x_{i_{depth(x)}} = x$ ,  $x_{i_{depth(x')}} = x'$ , set  $P'_{X_{i_{j+1}}} = e_{j+1}(H_2\left(x_{i_{j+1}}\right), P'_{X_{i_j}})$  and  $\tilde{C}^{(4)}_{x'} = P'_{x'}$ ;
- Let  $\tilde{C}^{(1)} = C^{(1)}$ ,  $\tilde{C}^{(2)} = C^{(2)}$ ,  $\tilde{C}_{at}^{(3)} = C_{at}^{(3)}$ .

#### **Updated ciphtext:**

$$\mathsf{cph'=}(\mathsf{S},\mathsf{R'},\tilde{\mathcal{C}}^{(1)},\tilde{\mathcal{C}}^{(2)},\{\tilde{\mathcal{C}}_{\mathsf{at}}^{(3)}\}_{\mathsf{at}\in\mathsf{S}},\{\tilde{\mathcal{C}}_{x\prime}^{(4)}\}_{x\prime\in\mathsf{cover}(\mathsf{R'})})$$



 $X_7$  is the new revoked user, the ciphertext part for  $x_{14}$  needs to update to  $x_{11}$  and  $x_8$ 





#### Verification

Verify the following equations:

$$C^{(1)} = \tilde{C}^{(1)}, C^{(2)} = \tilde{C}^{(2)}$$

$$\forall at \in S, \tilde{C}_{at}^{(3)} = C_{at}^{(3)},$$

$$\forall x \in \text{cover}(R) \cap \text{cover}(R'), C_x^{(4)} = \tilde{C}_{\text{Check each level}}^{(4)}$$

If hold, proceed to verify whether  $\exists i, s.t.$ 

$$e_{depth(x')+1}\Big(C^{(2)}, \prod_{i=1}^{\eta} P_{x'_i}^{c_i}\Big) = e_{depth(x')+1}\Big(g_0, \prod_{i=0}^{\eta} (\tilde{C}_{x'}^{(4)})^{c_i}\Big),$$

where  $c_1, \dots, c_{\eta} \stackrel{R}{\leftarrow} Z_p, x_j' \in \text{cover}(R') - \text{cover}(R), \text{and } depth(x_j') = i, i = 1, \dots, d.$ 





# Thanks!